

7.3 Sample Means

When using qualitative data typically we use \hat{p} as our sample statistic. When using quantitative data we use \bar{X} , the sample mean.

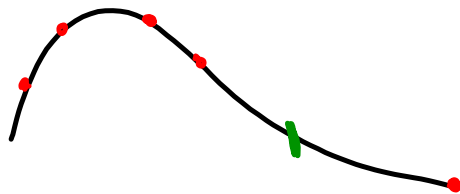
Mean + Standard deviation of the sampling distribution of \bar{x}

Suppose \bar{x} is the mean of a SRS of size n drawn from a large population. Assume the sample has mean μ and standard deviation σ .

The mean of the sampling distribution of \bar{x} is $\mu_{\bar{x}} = \mu$

The standard deviation of the sampling distribution of

$$\bar{x} \text{ is: } \sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} \quad , \quad 10\% \text{ condition must be met}$$



Sampling from a Normal Distribution

Suppose that a population has the $N(\mu, \sigma)$ distribution. Then the Sampling distribution has the normal distribution with mean μ and standard deviation of σ/\sqrt{n} (10% condition).

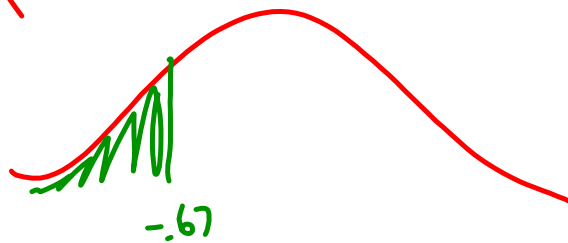
Ex: At the nutty Peanut company, shelled peanuts are placed in jars by a machine. The distribution of weights approximately follow the $N(16.1, .15)$ distribution.

- a) What is more likely: randomly drawing 1 jar and its weight is less than 16 oz. or randomly selecting 10 jars and finding average weight is less than 16 oz?
- b) Find the probability that a randomly selected jar has less than 16 oz.

$$P(X < 16) = P\left(z < \frac{X - \mu}{\sigma}\right)$$

normalcdf(lowerbound: -9999, upperbound: 16, $\mu = 16.1$, $\sigma = .15$)

$$= .2525$$



Ex: Find the probability 10 randomly selected jars contain less than 16 oz. on average.

$$P(\bar{X} < 16) \quad z = \frac{\mu_{\bar{x}} - \mu}{\sigma/\sqrt{n}} = \frac{16 - 16.1}{.15/\sqrt{10}} = -.2108$$

$$P(z < -.2108) = .4168$$

Central Limit Theorem (CLT)

Draw an SRS of size n from any population mean μ and finite standard deviation σ . The Central Limit Theorem says that when n is large, the sampling distribution of the sample mean, \bar{X} , is Normal.

Normal/Large Sample conditions for \bar{x} .

- If the population is Normal, so is the sampling distribution of \bar{x} regardless of sample size n .
- If the population is NOT Normal, CLT tells us the sampling distribution of \bar{x} will be approximately Normal if $n \geq 30$.

Suppose the number of texts sent during a typical day by students at a large school follows a right skewed distribution with $\mu = 45$ and $\sigma = 35$. How likely is it that an SRS of 50 students will have sent more than 2500 texts in the 1st day?

Large school, and $n \geq 30$, since its an SRS 50.

$$P(\bar{x} > \frac{2500}{50}) = P(\bar{x} > 50)$$

$$z = \frac{50 - 45}{35/\sqrt{50}}$$

$$z = 1.01$$

$$P(z > 1.01)$$

$$1 - P(z \leq 1.01)$$

$$.16$$

• 16% they will have sent more than 2500 texts

