

## 9.3 Tests about a population mean

### Conditions

- ① Random
- ② 10% condition
- ③ Large counts:  $n \geq 30$ , if  $n < 30$  we will graph to assess for skew or outliers

Test statistic: for means, we use the t-statistic which is the standardized value of how far the sample diverges from the parameter value ( $H_0$ ).

$$\text{test statistic} = \frac{\text{statistic} - \text{parameter}}{\text{standard deviation of the statistic}}$$

$$t = \frac{\bar{x} - \mu_0}{s_x / \sqrt{n}} \quad \text{where } H_0: \mu = \mu_0$$

Ex: A rock music radio station claims to play 50 minutes of music per hour. However, whenever you listen you feel like your listening to a commercial.

We want to test:

$$H_0: \mu = 50$$

$$H_a: \mu < 50$$

if  $\bar{x} = 47.9$  and  $s_x = 2.81$  using a sample of 12 hours of music.

$$t = \frac{\bar{x} - \mu_0}{s_x / \sqrt{n}} = \frac{47.9 - 50}{2.81 / \sqrt{12}} = -2.59$$

on table  
 $t = 2.59$

in between P values of .02 and .01.



### One sample t test for a mean

Suppose conditions are met. To test  $H_0: \mu = \mu_0$

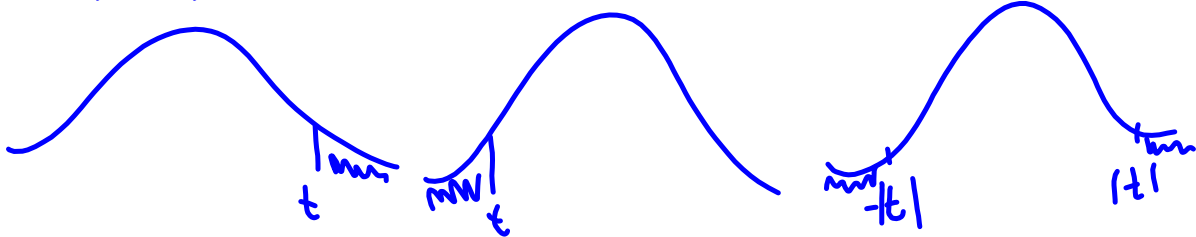
Compute 
$$t = \frac{\bar{x} - \mu_0}{\frac{s_x}{\sqrt{n}}}$$

Find the P value by calculating the probability of getting a t-statistic as large or larger in the direction of  $H_a$  in the  $t_{n-1}$  distribution.

$$H_a: \mu > \mu_0$$

$$H_a: \mu < \mu_0$$

$$H_a: \mu \neq \mu_0$$



check your understanding p. 583

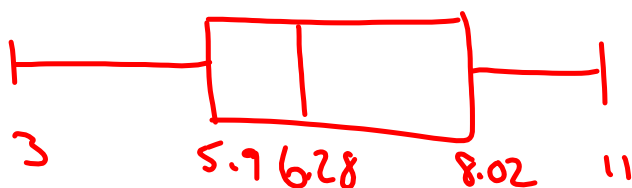
$$H_0: \mu = 8$$

$$H_a: \mu < 8$$

$\mu$  = average hours of sleep for students in college  
We are testing the claim at a significance level of .05.

conditions

- Random
- 28 students in less than 10% of all college students so 10% cond. is met.
- large counts. since  $28 < 30$  we graph



so no skew or outliers so it is roughly normal.

we will perform a 1 sample t test for  $\mu$

$$t = \frac{6.64 - 8}{1.98 / \sqrt{28}} = -3.63$$

$$P\text{value: } .00058$$



We will reject the  $H_0$  since  $.00058 < .05$   
So there is convincing evidence that the people in college get less than 8 hrs. sleep each night.

The 2 sided significance test for  $\mu$  at the  $\alpha$  significance level gives us similar information as the  $100(1-\alpha)\%$  CI.

Ex: check your understanding p. 586.

① P value = .275     $H_0: \mu = 128$      $H_a: \mu \neq 128$

$\alpha = .05$   
Fail to reject the  $H_0$  because  $.275 > .05$  meaning there is not convincing evidence the blood pressure differs from 128 in males from 35-44

② CI = (126.43 to 133.43)

Paired Data: data from study designs that involve making 2 observations on the same individuals or 1 observation of 2 similar individuals.

When paired data result from measuring the same quantitative variable twice we can make comparisons by analyzing differences in each pair. We can use 1 sample  $t$  procedures to perform inferences about the mean difference,  $\mu_d$ . This is often called pair  $t$  procedures

## Using Tests Wisely

### ① Determine Sample size

- significance level  $\rightarrow$  how much Type I error and type II are you capable of dealing with.  
 $\downarrow \alpha$ ,  $\downarrow P(\text{type I error})$  but  $\uparrow P(\text{Type II error})$
- Effect size: how large of a difference be  $H_0$  and the actual value is important to detect.  
 smaller difference = larger sample



- Power: higher Power = larger sample to give a better chance of detecting a difference when there is one.

② Statistical significance is not the same as practical importance.

③ Beware of multiple analyses.