

AP Test Review – Modeling Distributions of Data

I. Measuring Position

- A. Percentiles – p % of the observations are *less than* it.
- B. Cumulative Relative Frequency Graph
- C. z-scores
 - a) standardizes observations from distributions
 - b) tells how many standard deviations from the mean and in which direction
 - c) $z = \frac{x - \text{mean}}{\text{standard deviation}}$

You can calculate a z-score for any distribution, but area/proportion/p-value are for Normal Distributions

D. Transformations of Data

- A. Adding (Subtracting) a constant
 - a) adds (subtracts) to a measure of center or location
 - b) does not change measure of spread nor the shape of distribution
- B. Multiplying (Dividing) a constant
 - a) multiplies (divides) measure of center or location and spread
 - b) does not change shape of distribution

II. Density Curves

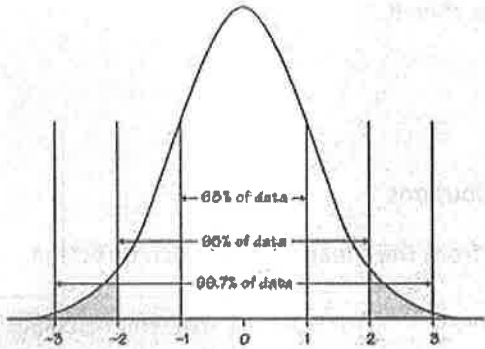
- A. Total Area = 1
- B. Area = proportion of observations in the interval of the values
- C. Always above or on x axis
- D. Mean
 - a) μ
 - b) located by eye, it is the balancing point
 - c) equal to median in symmetric curve, further out on skewed curves
- E. Median divides the area of the curve in half
- F. Standard Deviation
 - a) σ
 - b) turning point in symmetric curve, can't be located if it isn't symmetric

III. Normal Distribution

- A. bell shaped, symmetric density curve

B. has mean μ and standard deviation σ

C. 68-95-99.7 rule



D. $z = \frac{x - \mu}{\sigma}$

E. Table A – Gives the area to the LEFT of a z-score under the Normal curve

Common Mistakes:

- all z-scores do not need to come from a Normal distribution
- z-scores do not have the same units as the distribution they come from. Rather, a z-score of 2.3 means “2.3 standard deviations from the mean”.
- Notation: a Normal distribution with mean, μ , and standard deviation, σ , can also be written as $N(\mu, \sigma)$
- When calculating proportions/percentiles/area/probabilities from the Normal curve using technology or Table A, watch out for the direction (think inequality symbol) you are measuring.