

85.

$$\frac{(2a-5) \cancel{(a+9)(a+9)}}{\cancel{a-9} \cdot \cancel{a+9}} + \frac{(9) \cancel{(a-9)(a+9)}}{\cancel{a+9} \cdot \cancel{(a-9)(a+9)}} = \frac{(-6) \cancel{(a-9)(a+9)}}{\cancel{a+9} \cdot \cancel{(a-9)(a+9)}}$$

$$\frac{\text{LCD}}{(a-9)(a+9)}$$

$$(2a-5)(a+9) + a(a-9) = -6$$

$$2a^2 + 18a - 5a - 45 + a^2 - 9a = -6$$

$$3a^2 + 4a - 45 = -6$$

$$3a^2 + 4a - 39 = 0$$

$$(3a+13)(a-3) = 0$$

$$3a+13=0$$

$$\frac{3a}{3} = \frac{-13}{3}$$

$$a = \frac{-13}{3}$$

$$a-3=0$$

$$a=3$$

$$0-3+$$

$$4-6 \checkmark$$

$$71-$$

### 3-3 Study Guide and Intervention

#### Properties of Logarithms

**Properties of Logarithms** Since logarithms and exponents have an inverse relationship, they have certain properties that can be used to make them easier to simplify and solve.

If  $b$ ,  $x$ , and  $y$  are positive real numbers,  $b \neq 1$ , and  $p$  is a real number, then the following statements are true.

•  $\log_b xy = \log_b x + \log_b y$  Product Property

•  $\log_b \frac{x}{y} = \log_b x - \log_b y$  Quotient Property

•  $\log_b x^p = p \log_b x$  Power Property

expand

②

①

③

condense

②

③

①

**Example 1** Evaluate  $3 \log_2 8 + 5 \log_2 \frac{1}{2}$ .

$$\begin{aligned} 3 \log_2 8 + 5 \log_2 \frac{1}{2} &= 3 \log_2 2^3 + 5 \log_2 2^{-1} \\ &= 3(3 \log_2 2) + 5(-\log_2 2) \\ &= 3(3)(1) + 5(-1)(1) \\ &= 4 \end{aligned}$$

$$8 = 2^3; 2^{-1} = \frac{1}{2}$$

Power Property

$$\log_2 x = 1$$

Simplify.

**Example 2** Expand  $\ln \frac{8x^5}{3y^2}$ .

$$\begin{aligned} \ln \frac{8x^5}{3y^2} &= \ln 8x^5 - \ln 3y^2 \\ &= \ln 8 + \ln x^5 - \ln 3 - \ln y^2 \\ &= \ln 8 + 5 \ln x - \ln 3 - 2 \ln y \end{aligned}$$

Quotient Property

Product Property

Power Property

**Exercises**1. Evaluate  $2 \log_3 27 + 4 \log_3 \frac{1}{3}$ .

$$\log_3 27^2 + \log_3 \frac{1}{3^4}$$

$$\log_3 27^2 \cdot \frac{1}{3^4}$$

$$\log_3 9 = \log_3 3^2$$

$$3^y = 9$$

$$y = 2$$

Expand each expression.

2.  $\log_3 \frac{5r^5}{\sqrt[3]{t^2}}$ 

$$= \log_3 5r^5 - \log_3 \sqrt[3]{t^2}$$

$$= \log_3 5 + \log_3 r^5 - \log_3 \sqrt[3]{t^2}$$

3.  $\log \frac{(a-2)(b+4)^6}{9(b-2)^4}$ 

$$= \log_3 5 + 5 \log_3 r - \frac{2}{3} \log_3 t$$

Condense each expression.

4.  $11 \log_9 (x-3) - 5 \log_9 2x$ 5.  $\frac{3}{4} \ln (2h-k) + \frac{3}{5} \ln (2h+k)$ 

$$= \ln (2h-k)^{\frac{3}{4}} + \ln (2h+k)^{\frac{3}{5}}$$

$$= \ln (2h-k)^{\frac{3}{4}} (2h+k)^{\frac{3}{5}}$$

$$= \ln \sqrt[4]{(2h-k)^3} \sqrt[5]{(2h+k)^3}$$

### Properties of Logarithms

**Change of Base Formula** If the logarithm is in a base that needs to be changed to a different base, the **Change of Base Formula** is required.

For any positive real numbers  $a$ ,  $b$ , and  $x$ ,  $a \neq 1$ ,  $b \neq 1$ ,  $\log_b x = \frac{\log_a x}{\log_a b}$ .

Many non-graphing calculators cannot be used for logarithms that are not base  $e$  or base 10. Therefore, you will often use this formula, especially for scientific applications. Either of the following forms will provide the correct answer.

$$\log_b x = \frac{\log x}{\log b}$$

$$\log_b x = \frac{\ln x}{\ln b}$$

**Example** Evaluate each logarithm.

a.  $\log_2 7$

$$\log_2 7 = \frac{\ln 7}{\ln 2} \quad \text{Change of Base Formula}$$

$$\approx 2.81 \quad \text{Use a calculator.}$$

b.  $\log_{\frac{1}{3}} 10$

$$\log_{\frac{1}{3}} 10 = \frac{\log 10}{\log \frac{1}{3}} \quad \text{Change of Base Formula}$$

$$\approx -2.10 \quad \text{Use a calculator.}$$

**Exercises**

Evaluate each logarithm.

$$1. \log_{32} 631 = \frac{\log 631}{\log 32} \\ = 1.86$$

$$2. \log_3 17 = \frac{\ln 17}{\ln 3} \\ = 2.58$$

3.  $\log_7 1094$

4.  $\log_6 94$

5.  $\log_5 256$

6.  $\log_9 712$

7.  $\log_6 832$

8.  $\log_{11} 47$

9.  $\log_3 9$

10.  $\log_8 256$

11.  $\log_{12} 4302$

12.  $\log_{0.5} 420$

HW: p. 185, #1-15 odd, 18, 19-31 odd, 43, 49, 53, 59, 63